Name:	Class:	Class Register Number:



Chung Cheng Figh School Chung Cheng Figh School Chung Gheng Figh School Chung Cheng Figh School Chung

Parent's Signature

PRELIMINARY EXAMINATION 2021 SECONDARY 4

MATHEMATICS

4048/01

Paper 1

Wednesday 15 September 2021

2 hours

Candidates answer on the Question Paper.

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 80.

For Examiner's Use		
Total	/ 80	

This document consists of 19 printed pages and 1 blank page.

Mathematical Formulae

Compound interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = $\pi r l$

Surface area of a sphere = $4 \pi r^2$

Volume of a cone =
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere =
$$\frac{4}{3}\pi r^3$$

Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

Arc length = $r \theta$, where θ is in radians

Sector area =
$$\frac{1}{2}r^2\theta$$
, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$Mean = \frac{\sum f x}{\sum f}$$

Standard deviation =
$$\sqrt{\frac{\sum f x^2}{\sum f} - \left(\frac{\sum f x}{\sum f}\right)^2}$$

3 Answer all the questions.

1 State which of the following number(s) is/are irrational.

$$0.5^{\circ}, \ \frac{\pi}{2}, \ 2\sqrt{2}, \ 3\sqrt{3} \times \sqrt{3}$$

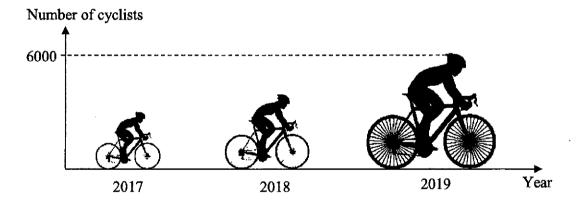
Answer	*****	ſ	1	٦	

2 x is an integer greater than 1. Write the following in order of size, starting with the largest.

$$x^0$$
, $x^{-\frac{3}{2}}$, $x^{\frac{3}{4}}$, $x^{\frac{3}{2}}$

Answer		[1
--------	--	----

3 The graph shows the number of cyclists in an annual cycling marathon for the years 2017 to 2019.



(a)	State one aspect of the	e graph that may be	misleading
-----	-------------------------	---------------------	------------

	[1]
Explain how this may lead to a miginterpretation of the graph	

(b) Explain how this may lead to a misinterpretation of the graph.

.....[1]

4	(a)	Simplify	$\left(\frac{2^{a-1}\sqrt{2}}{2^a}\right)^2$
---	-----	----------	--

Answer		[2]
AATRO IT C.	***************************************	L-

(b) If $27m^{3x} = 1$ and m > 0, find $m^{2x} + m^{-x}$.

Answer	*************************	[2]

Show that, for all n, $(5n+3)^2 - (5n-3)^2$ is a multiple of 4.

6 Gladys wrote down four numbers. The mean of these numbers is 13, the median is 12 and the mode is 10. Find the four numbers.			
		Answer[2]	
7	(a)	Mrs Boey deposited \$20 000 in a bank that pays 0.8% per annum compound interest compounded half-yearly. Find the total amount of money she will receive at the end of 5 years, leaving your answer to the nearest cent.	
		Answer[2]	
	(b)	Singapore Budget 2018: GST to be raised from 7% to 9% some time between 2021 and 2025	
		Shane and Glen came across an article in the newspaper with the headline shown above and made the following comments. Shane: Oh no, the GST will increase by 2% soon! Glen: No! I disagree. It did not increase by 2%, in fact it is MORE than 2%!	
		Whose statement is correct? Support your answer with mathematical calculations.	
		Answer[2]	

8	(a)	Find the range of values of x which satisfy the inequalities
---	-----	--

$$\frac{17-8x}{3} < \frac{2(3x-1)}{5} \le 4.$$

Answer	[3]
Hence, state the smallest prime number that satisfies the inequalities.	
Answer	[1]
	Hence, state the smallest prime number that satisfies the inequalities.

9 (a) Factorise completely $9b^2 - 6ab + a^2 - x^2$.

Answer[2]

(b) Simplify $\frac{5}{2x^2-7x-4} - \frac{8}{4-x}$.

Answer [3]

Roy made a model of his yacht with a scale of 1: 40.

(a)	The actual length of the yacht is 12.5 m, find the length of the model in cm.
	Answercm [1]
(b)	Roy wants to spray paint his yacht. He can select either of the following options to paint his yacht.
	Option A: A lump sum payment of \$1 000
	Option B: Payment for cost of paint at \$5.50 per m ²
	[Cost of manpower is included in both options]
	If the total surface area of the model to be painted is 937.5 cm ² , find the surface area
	of his yacht. Which one of the two options should Roy select to paint his yacht?
	[Show your workings clearly]
	•••••••••••••••••••••••••••••••••••••••
	[3]

11 $\xi = \{x : x \text{ is an integer and } 1 \le x \le 10\}$

 $A = \{x : x \text{ is a factor of } 20\}$

 $B = \{x : x \text{ is a perfect square}\}$

Find

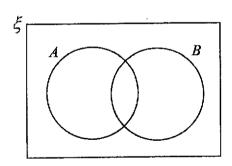
(a) n(B),

Answer[1]

(b) $A' \cap B'$.

Answer[1]

(c) On the Venn Diagram, shade the region which represents $(A \cup B)' \cup (A \cap B)$.



[1]

12 When written as the product of their prime factors,

$$p \text{ is } 2^2 \times 3 \times 5,$$

q is
$$2^6 \times 3^3$$
,

r is
$$2^2 \times 3^2 \times 11$$
.

Find

(a) the value of the cube root of q,

Amornon		Г1	1
Answer	*****************************	L	1

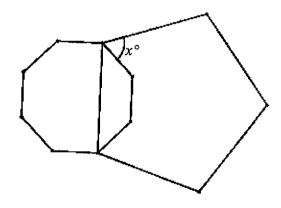
(b) the LCM of p, q and r, giving your answer as the product of its prime factors,

4	1	г 1 1	3
Answer	***************************************	LT.	ļ

(c) the greatest number that will divide p, q and r exactly.

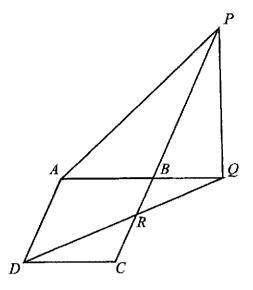
A		T 1	1	
Answer	***************************************	11	.	İ

13 The diagram shows a regular pentagon and a regular octagon. Calculate the value of x.



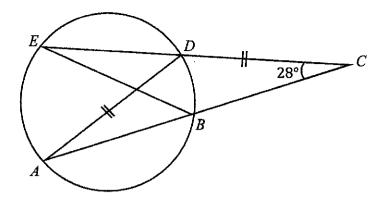
Answer x	=		[3]	i
----------	---	--	----	---	---

14 The diagram shows a rhombus ABCD. ABQ, PBC and DRQ are straight lines and AQ = BP.



(a) State the triangle that is similar to triangle BRQ.

	Answer Triangle [1]
(b)	Prove that triangle DQA is congruent to triangle APB.
	······
	[2]



A, B, D and E are points on the circle such that AD = CD and angle $BCD = 28^{\circ}$. Explain with geometrical reasons, why the length of BC equals to BE.

The masses of 20 bags, in kg, are measured.

The results are shown on the stem-and-leaf diagram.

Mass of 20 bags

Stem	Leaf
0	9
1	2
2	0666
3	0 3 3 4 4 8 8 1 2 9 9 9
4	12999
5	0 1

Key: 0|9 means 0.9 kg

(a) Find the mean mass of the ba	ıgs.
----------------------------------	------

	Answerkg [1]					
(b)	Find the standard deviation of the masses of the bags.					
	Answerkg [1]					
(c)	It was found later that the weighing machine has an error.					
	Each bag was actually 0.08 kg heavier. Explain how this will affect the mean and standard deviation.					
	[2]					

- 17 y is inversely proportional to the square of x, x > 0.
 - (a) If x is increased by 25%, find the percentage change in y.

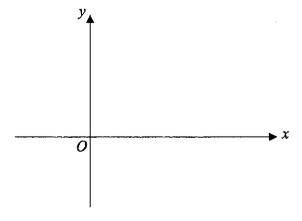
Answer% [2]

- **(b)** Given that y = 16 when $x = \frac{1}{2}$, find
 - (i) the equation connecting y and x,

Answer[2]

(ii) the value of x when y = 100.

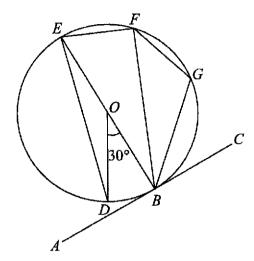
(c) Sketch the graph which represents the relation between y and x.



[1]

18	In the	e following sequence,
-		$(1\times 2)-2=0$
		$(2\times3)-4=2$
		$(3\times4)-6=6$
		$(4\times5)-8=12$
		$(a\times 12)-b=c$
		$(d\times e)-f=g$
	(a)	Find the values of a , b and c .
	•	
		Answer $a =, b =, c =$ [2]
	(b)	Express g in terms of d .
	` '	
		Answer[2]
	(c)	Explain why 279 cannot be the result of an equation in this sequence.

The diagram shows a circle BDEFG, centre O and diameter BE. The line AC is a tangent to the circle at B and angle $BOD = 30^{\circ}$. The ratio of angle EBF to angle FBG to angle GBC is 1:1:2.



(a)	State a fact about the arcs EF and FG .
	[1]
(b)	Showing all reasons clearly, find (i) angle <i>DEB</i> ,
	Answer[1]

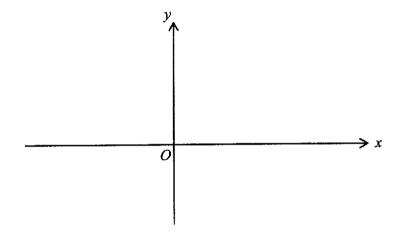
(ii) angle EFG.

Answer	***************************************	[2]
--------	---	-----

20 (a) Express $-x^2 + 4x + 12$ in the form -(x+p)(x-q).

4	4======================================	Г13	
Answer	4*****************************		

(b) Sketch the graph of $y = -x^2 + 4x + 12$ on the axes below. Indicate clearly the values where the graph crosses both axes. [2]



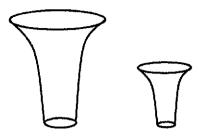
(c) Find the coordinates of the turning point.

Answer ((,)	[1]

(d) Without solving the equation algebraically, explain why $-x^2 + 4x + 12 = 18$ has no solution.

.....[1]

21 The diagram shows two geometrically similar containers. The cost of painting the base area of the smaller container is $\frac{25}{64}$ of the cost of painting the base of the larger container.

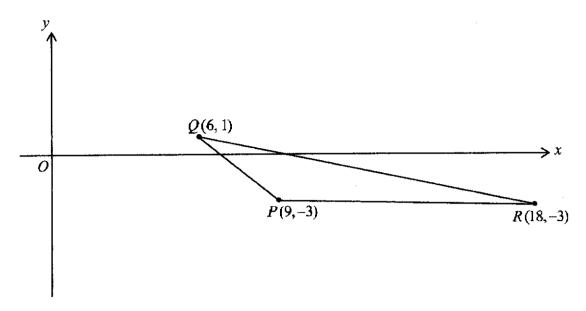


(a) The top of the larger container has a circumference of 24 cm. Find the circumference of the top of the smaller container.

Answer cm [2]

(b) The capacity of the smaller container is 0.45 litres.Find the capacity of the larger container, giving your answer to 2 decimal places.

Answerlitres [1]



In the diagram, the points P, Q and R have coordinates (9,-3), (6,1) and (18,-3) respectively.

(a) Find the length of PQ.

Answer	units	[1]

(b) Find the value of $\cos \angle QPR$, giving your answer as a fraction in its simplest form.

Answer[1]

(c) Find the area of triangle PQR.

Answerunits² [1]

	19
(d)	Find the equation of the line PQ .
	Answer[2]
(e)	The equation of a line passing through the point R is $4x + 21y = 9$.
	Find the coordinates of the point of intersection of this line and the line PQ .

Answer[3]

 \sim End of Paper \sim

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Name:	Class:	Class Register Number:





CHUNG CHENG HIGH SCHOOL (MAIN)

Chang Chang High School Chung Cheng High School Chung Chang High School Chung Chang Chang Chang Chang Chang High School Chung Chang
PRELIMINARY EXAMINATION 2021 SECONDARY 4

MATHEMATICS

4048/02

Paper 2

Wednesday 1 September 2021 2 hours 30 minutes

Candidates answer on the Question Paper

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use paper clips, glue or correction fluid.

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At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 100.

For Examiner's Use				
Question Number	Marks Obtained			
1				
2				
. 3				
4				
5				
6				
7				
8				
9				
10				
Total Marks				

This document consists of 21 printed pages and 1 blank page.

Mathematical Formulae

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$$P\left(1 + \frac{r}{100}\right)^n$$

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Curved surface area of a cone = $\pi r l$

Surface area of a sphere = $4 \pi r^2$

Volume of a cone =
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Volume of a sphere =
$$\frac{4}{3}\pi r^3$$

Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

Arc length = $r\theta$, where θ is in radians

Sector area =
$$\frac{1}{2}r^2\theta$$
, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$Mean = \frac{\Sigma fx}{\Sigma f}$$
Standard deviation =
$$\sqrt{\frac{\Sigma fx^2}{\Sigma f} - \left(\frac{\Sigma fx}{\Sigma f}\right)^2}$$

1 (a) Simplify
$$\left(\frac{a^6b^3}{8}\right)^{\frac{1}{3}} \div \frac{3b^{-1}}{a^2}$$
.

(b) Solve
$$\frac{2}{x-2} + \frac{3}{x+2} = 0$$
.

Answer
$$x = \dots$$
 [2]

(c) Make q the subject in the equation $pq+9=p^2+3q$ and simplify your answer.

(d) (i) Simplify $(4x+3y)^2 + (3x-4y)^2$.

Answer[2]

(ii) It is given that $x^2 + y^2 = 1$. Using your answer in part (i), explain why the maximum value of $(4x + 3y)^2$ is 25.

2	During nuclear fusion, it is observed that when two hydrogen atoms are fused
	together to form one helium atom, there is a loss in mass, M .
	The atomic masses of one hydrogen atom and one helium atom are given in the table
	below. The masses are given in atomic mass unit (u).

		Atom	Hydrogen	Helium		
		Atomic Mass (u)	2.0141	4.0026		
(a)	Find M (in	n u), leaving your ans	wer in standard for	rm.		
(b)	Express M	f as a percentage of the	Answer the atomic mass of	one helium atom.		[2]
(c)	Given tha	t 1 u = 1.66×10 ⁻²⁷ kg		ms.	%	[2]

- Town P and Town Q are 40 km apart. A car is travelling from Town P to Town Q at an average speed of x km/h. During its return journey, the car later travelled back to Town P from Town Q at an average speed of (x+8) km/h and the time taken for the return journey was 12 minutes less.
 - (i) Write down an equation to represent this information and show that it simplifies to $x^2 + 8x 1600 = 0$.

Answer

[4]

(ii) Solve the equation $x^2 + 8x - 1600 = 0$, giving your solutions correct to two decimal places.

Answer
$$x =$$
 or [3]

(iii)	Given that the car left Town P at 0900, find the time when the car reached Town
	Q. Give your answer correct to the nearest minute.

Answer[2]

4 The variables x and y are connected by the equation $y = \frac{3}{2}x + \frac{5}{x} - 7$. Some corresponding values of x and y are given in the table below.

x	0.5	1	1.5	2	3	4	5	6	7
y	3.75	-0.5	-1.42	p	-0.83	0.25	1.5	2.83	4.21

(a)	Find	the	value	of p .
-----	------	-----	-------	----------

[1]

Answer
$$p = \dots$$

(b) On the grid opposite, draw the graph of $y = \frac{3}{2}x + \frac{5}{x} - 7$ for $0.5 \le x \le 7$.

Use the scale of 2 cm to represent 1 unit on both axes.

[3]

(c) By drawing a tangent, find the gradient of the curve at x = 2.5.

Answer[2]

(d) (i) On the grid in part (b), draw the line 2y + x = 2 for $0 \le x \le 7$.

[2]

(ii) Write down the x-coordinates of the points where the line intersects the curve.

Answer
$$x =$$
 or [2]

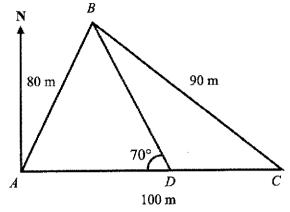
(iii) Show that the points of intersection of the line and the curve give the solutions to the equation $2x^2 - 8x + 5 = 0$.

Answer[2]

		1					
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5 The diagram below shows three points, A, B and C on flat ground.

AB = 80 m, AC = 100 m and BC = 90 m. C is due east of A.



(a) (i) Show that angle $ACB = 49.5^{\circ}$, correct to one decimal place.

[3]

(ii) Hence, calculate the bearing of C from B.

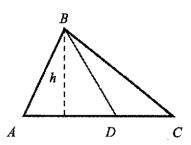
Answer° [2]

(iii) Point D lies along AC such that angle $BDA = 70^{\circ}$. Find the distance CD.

Answer m [3]

(iv)	Find the ratio of area of triangle ABD to area of triangle BDC.
	Give your answer correct to one decimal place.

Since they share a common height,

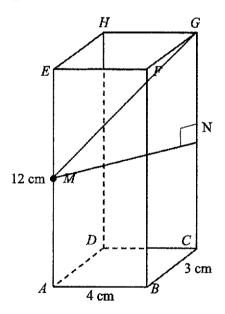


Answer		[2]
--------	--	-----

(b) The diagram below shows a cuboid with rectangular base ABCD.

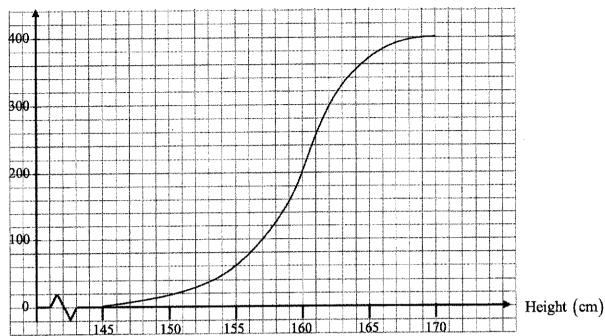
AB = 4 cm, BC = 3 cm and AE = 12 cm. M is the midpoint of AE.

Find the angle of elevation of G from M.



Answer	***************************************	[3]
--------	---	-----

6 (a) The heights of 400 students in School A are recorded. The cumulative frequency curve below shows the distribution of their heights.



(i) State the median.

Cumulative frequency

Answer	 cm	[1]
211001701	 	- 1

(ii) Find the interquartile range of the distribution.

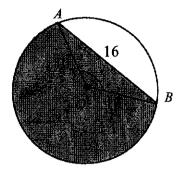
(iii) In School B, the median and interquartile range of the heights of another 400 students are 165 cm and 8 cm respectively. Make two comments comparing the heights of students in School A and School B.

Answer

[2]

(b)	John flipped a coin five times and obtained five successive heads. Is it conclusive that the coin is biased? Explain your answer clearly.					
	Answ	er				
	obtai	given that John only flipped ning 5 successive heads whit ogical conclusion that the co	ch is still possible.			
			*********			[2]
(c)		vo-digit number is formed	•		· ·	
		nother random card from	-			
		'3'. Bag B contains three (
	'15'.	ving a '1' and "5" from Ba	ig A and dag b res	specuvery	will form the number	
	(i)	Complete the possibility	diagram below.			
	(-)					
		$\operatorname{Bag} B \setminus \operatorname{Bag} A$	1	2	3	
		4	14			
		5	III	25		
		7				
		, as a fraction in its simple ted is	est form, the proba	bility that	the two-digit number	[2]
	(ii)	odd,				
	(iii)	a perfect square,	Answer			[1]
	(iv)	a prime number,	Answer	•••••	•••••••••••••••••••••••••••••••••••••••	[1]
	(v)	a factor of 135.	Answer		•••••••••••••••••••••••••••••••••••••••	[1]
			Answer			[2]
						r-J

7 The diagram shows a circle, centre O, radius 10 cm. AB is a chord of length 16 cm.



(a) Show that angle AOB = 1.855 radians, correct to four significant figures.

Answer

[2]

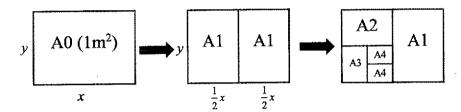
Hence, find the

(b) perimeter of the shaded segment,

(c) area of the shaded segment.

 A piece of A0-sized paper has a total surface area of 1 m^2 . The length and breadth of the A0-sized paper are x m and y m respectively.

An A1 paper is an A0 paper folded in half, length-wise. An A2 paper is an A1 paper folded in half, so on and so forth.



(i) Write down the relationship between x and y.

Answer	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	[1]

(ii) Given that all A-sized papers are geometrically similar, show that $\frac{x}{y} = \sqrt{2}$.

[2]

(iii) Hence, using parts (i) and (ii), find the values of x and y.

(IV)	write down the dimensions of an A4-sized paper in millimetres.	
	<i>Answer</i> mm × mm	[2]
(v)	Given that N is an integer, express the number of pieces of AN-sized paper that	
	can be cut out from an A0-sized paper in terms of N.	
	Answer	[1]

9 Robert has 3 options to get to school every weekday morning.

Option A: He takes the bus.

Option B: He takes the MRT.

Option C: He takes a taxi.

The matrices A, B and C represent his journey to school if he were to choose option

A, B or C respectively.

						Taxi			
	(1	0	0)	(0	0	0)	0	0	. 0
A =	0	0	0 , B =	0	1	0 , C =	0	0	0 .
	0	0	0	0	0	$\begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$, $\mathbf{C} =$	0	0	1)

(a) In a particular week, Robert took the bus 3 times. He took the MRT and taxi in each of the other two days. The above information can be represented by a matrix S where S = 3A + B + C. Find S.

Answer[2]

(b) The table below shows the travelling time taken, in minutes, for each of the 3 options that Robert can take to get to school.

Option	Bus	MRT	Taxi
Time taken (in minutes)	30	20	15

(i) Write down a column matrix N to represent the information in the table.

Answer $N = \dots$ [1]

(ii) Eva	luate the	matrix	SN.
----------	-----------	--------	-----

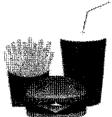
		Answer $SN = \dots$	[2]
	(iii)	State what the elements in matrix SN represent.	
		Answer	
		The elements represent the total time taken in minutes, in that particular	
		week by Robert to go to school by via option A , B and C respectively.	

			[1]
(c)	Write	down a matrix J such that product of J and the answer in part (b)(ii) will	
	give	he average travelling time taken by Robert in a particular week.	
		Answer	[1]
(d)	Henc week	e, find the average travelling time taken by Robert per day in a particular	

Answer minutes

[2]

10 The diagram below shows the menu from a fast food restaurant.



Combo A

- Burger
- Medium Fries
- Medium Drink

\$5.90 only!

Upsize your drink and fries to Large-size for only \$1.10

Ala carte	Medium (\$)	Large (\$)
Burger (1 size)	3.2	:0
Fries	2.20	2.90
Drink	2.80	3.60

(a) Albert wants to buy a burger for both himself and his brother Bart. His brother wants at least a medium-sized fries. Albert wants a large drink while Bart wants a medium drink.

By considering three options, suggest how Albert should place his order. Justify any decisions that you make and show your calculations clearly.

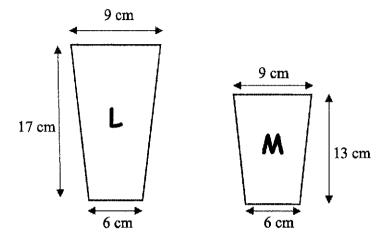
Answer

Choose 3 out of the 4 possible options

[4]

OR He should choose Option C as for \$0.20 more, he can get an extra packet of medium fries so it is the most value – for – money option.

(b) The diagram below shows the cross-sectional area of the large (L) and medium (M) drink cups sold by the fast food restaurant in part (a). The Large and Medium cups have a height of 17 cm and 13 cm respectively. The top and bottom diameters of both cups are 9 cm and 6 cm respectively



The volume of a cup is given by $V = \frac{1}{3}\pi h(R^2 + Rr + r^2)$ where h is the height,

R and r are the radii of the top and bottom of the cup respectively. Using the information from part (a), determine whether the medium cup or large cup gives better value for money.

Answer

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Name:	Class:	SOLUTIONS



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Parent's Signature

PRELIMINARY EXAMINATION 2021 SECONDARY 4

MATHEMATICS

4048/01

Paper 1 Wednesday 15 September 2021

2 hours

Candidates answer on the Question Paper.

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 80.

For Examiner's Use					
Total	/ 80				

This document consists of 19 printed pages and 1 blank page.

[Turn over

Mathematical Formulae

Compound interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = $\pi r l$

Surface area of a sphere = $4 \pi r^2$

Volume of a cone =
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere =
$$\frac{4}{3}\pi r^3$$

Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

Arc length = $r\theta$, where θ is in radians

Sector area =
$$\frac{1}{2}r^2\theta$$
, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$Mean = \frac{\sum f x}{\sum f}$$

Standard deviation =
$$\sqrt{\frac{\sum f x^2}{\sum f} - \left(\frac{\sum f x}{\sum f}\right)^2}$$

3 Answer all the questions.

1 State which of the following number(s) is/are irrational.

0.5,
$$\frac{\pi}{2}$$
, $2\sqrt{2}$, $3\sqrt{3} \times \sqrt{3}$
 $\frac{\pi}{2}$, $2\sqrt{2}$

0.5 can be expressed as $\frac{5}{9}$, so 0.5 is a rational number

[1]

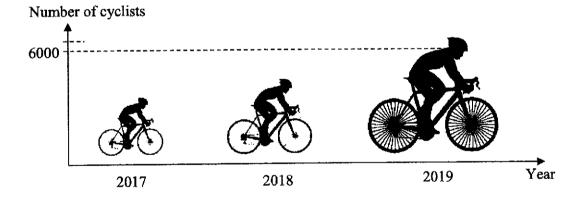
x is an integer greater than 1.Write the following in order of size, starting with the largest.

$$x^{0}, x^{-\frac{3}{2}}, x^{\frac{3}{4}}, x^{\frac{3}{2}}$$

$$x^{\frac{3}{2}}, x^{\frac{3}{4}}, x^{0}, x^{-\frac{3}{2}}$$

]	L		İ
	1	1	1

3 The graph shows the number of cyclists in an annual cycling marathon for the years 2017 to 2019.



- (a) State one aspect of the graph that may be misleading.

 The vertical axis is not labelled at the start / No "0" on the y-axis. OR

 The size of the picture not only increases with height, but also in the width.
- (b) Explain how this may lead to a misinterpretation of the graph.
 It is difficult to estimate the number of cyclists for 2017 and 2018. OR
 Unclear as to whether the height or the area is used to determine the number of cyclists

[Turn over

4

4 (a) Simplify
$$\left(\frac{2^{a-1}\sqrt{2}}{2^a}\right)^2$$
.

$$\left(\frac{2^{a-1}\sqrt{2}}{2^a}\right)^2 = \left(\frac{2^a \cdot 2^{-1} \cdot \sqrt{2}}{2^a}\right)^2$$
$$= \left(\frac{\sqrt{2}}{2}\right)^2$$
$$= \frac{2}{4}$$

 2^{-1} is considered as not simplified, need to simplify to $\frac{1}{2}$

Answer[2]

(b) If
$$27m^{3x} = 1$$
 and $m > 0$, find $m^{2x} + m^{-x}$.

$$27m^{3x} = 1$$

$$m^{3x} = \frac{1}{27}$$

$$m^{x} = \frac{1}{3}$$

$$m^{2x} + m^{-x} = \left(m^{x}\right)^{2} + \left(m^{x}\right)^{-1}$$
$$= \left(\frac{1}{3}\right)^{2} + \left(\frac{1}{3}\right)^{-1}$$
$$= 3\frac{1}{9}$$

Some obtained $m^{3x} = 3^{-3}$ and from this step, some went to equate m = 3 and x = -1 which is not always true as $m = \frac{1}{3}$, x = 1 or m = 9, $x = -\frac{1}{2}$.

As there are 2 unknown variables in this equation so we need two equations to be solved simultaneously in order to solve for the value of m and x.

Answer[2]

5 n is a positive integer.

Show that, for all n, $(5n+3)^2 - (5n-3)^2$ is a multiple of 4.

[2]

Answer

$$(5n+3)^{2} - (5n-3)^{2} = (5n+3+5n-3)(5n+3-(5n-3))$$

$$= (10n)(6)$$

$$= 60n$$

$$= 4(15n)$$

Since n is a positive integer and 60n = 4(15n), $(5n+3)^2 - (5n-3)^2$ is a multiple of 4.

Gladys wrote down four numbers. 6

> The mean of these numbers is 13, the median is 12 and the mode is 10. Find the four numbers.

Let the four numbers be a, b, c and d in ascending order. Since the mode is smaller than the median, a and b will be 10. Since median is 12,

$$\frac{10+c}{2} = 12$$

$$c = 24-10$$

$$= 14$$

Since mean is 13, $10+10+14+d=13\times 4$

$$d = 18$$

The four numbers are 10, 10, 14 and 18.

Answer[2]

Mrs Boey deposited \$20 000 in a bank that pays 0.8% per annum compound interest 7 (a) compounded half-yearly. Find the total amount of money she will receive at the end of 5 years, leaving your answer to the nearest cent.

Total amount =
$$$20000 \left(1 + \frac{0.8}{2(100)}\right)^{5\times2}$$

= $$20814.55468$
= $$20814.55$ (nearest cent)

Answer[2]

Singapore Budget 2018: GST to be raised from 7% to 9% **(b)** some time between 2021 and 2025

Shane and Glen came across an article in the newspaper with the headline shown above and made the following comments.

Shane: Oh no, the GST will increase by 2% soon!

Glen: No! I disagree. It did not increase by 2%, in fact it is MORE than 2%!

Whose statement is correct? Support your answer with mathematical calculations.

$$\frac{9-7}{7} \times 100\% = 28.6\% (3sf)$$

Percentage point is defined as the difference between two percentages. So the increase from 7% to 9% is two percentage points, and not two percent.

Glen's statement is correct as the GST will increase by 28.6%, which is more than 2%.

Answer[2]

Turn over

8 (a) Find the range of values of x which satisfy the inequalities

$$\frac{17-8x}{3} < \frac{2(3x-1)}{5} \le 4.$$

$$\frac{2(3x-1)}{5} \le 4$$

$$3x-1 \le 10$$

$$3x \le 11$$

$$x \le 3\frac{2}{3}$$
and
$$x > \frac{91}{58}$$

$$x > 1\frac{33}{58} < x \le 3\frac{2}{3}$$

$$\therefore 1\frac{33}{58} < x \le 3\frac{2}{3}$$

Answer[3]

(b) Hence, state the smallest prime number that satisfies the inequalities.

Smallest prime number is 2.

Answer[1]

9 (a) Factorise completely $9b^2 - 6ab + a^2 - x^2$.

$$9b^{2} - 6ab + a^{2} - x^{2} = (3b - a)^{2} - x^{2}$$
$$= (3b - a + x)(3b - a - x)$$
Or

$$9b^{2} - 6ab + a^{2} - x^{2} = (a - 3b)^{2} - x^{2}$$
$$= (a - 3b + x)(a - 3b - x)$$

Answer [2]

(b) Simplify $\frac{5}{2x^2-7x-4} - \frac{8}{4-x}$.

$$\frac{5}{2x^2 - 7x - 4} - \frac{8}{4 - x} = \frac{5}{(2x + 1)(x - 4)} + \frac{8}{x - 4}$$

$$= \frac{5 + 8(2x + 1)}{(2x + 1)(x - 4)}$$

$$= \frac{5 + 16x + 8}{(2x + 1)(x - 4)}$$

$$= \frac{16x + 13}{(2x + 1)(x - 4)}$$

Answer[3]

7

10	Roy made a model	of his	yacht with	a scale	of	1:	4(J
----	------------------	--------	------------	---------	----	----	----	---

(a) The actual length of the yacht is 12.5 m, find the length of the model in cm.

1:40

1 cm: 0.4 m

Length of model =
$$\frac{12.5}{0.4}$$

= 31.25 cm

The value 31.25 is exact, so it should not be expressed as 31.3 (correct to 3 s.f.)

(b) Roy wants to spray paint his yacht. He can select either of the following options to paint his yacht.

Option A: A lump sum payment of \$1 000 Option B: Payment for cost of paint at \$5.50 per m² [Cost of manpower is included in both options]

If the total surface area of the model to be painted is 937.5 cm², find the surface area of his yacht. Which one of the two options should Roy select to paint his yacht? [Show your workings clearly]

1 cm: 0.4 m 1 cm²: (0.4)² m² 1 cm²: 0.16 m²

Cost of paint =
$$937.5 \times 0.16 \times $5.50$$

= $$825$

Roy should select Option B as it is cheaper.

Answer[3]

11 $\xi = \{x : x \text{ is an integer and } 1 \le x \le 10\}$ $A = \{x : x \text{ is a factor of } 20\}$ $B = \{x : x \text{ is a perfect square}\}$

Find

(a) n(B), $\xi = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ $A = \{1, 2, 4, 5, 10\}$ $B = \{1, 4, 9\}$ ** 1 is a perfect square n(B) = 3

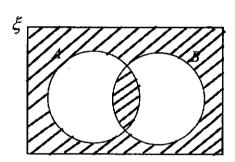
Answer[1]

(b) $A' \cap B'$.

 $A' \cap B' = \{3, 6, 7, 8\}$ It is a set, so curly brackets must be included.

Answer[1]

(c) On the Venn Diagram, shade the region which represents $(A \cup B)' \cup (A \cap B)$.



[1]

9

12 When written as the product of their prime factors,

p is
$$2^2 \times 3 \times 5$$
,
q is $2^6 \times 3^3$,
r is $2^2 \times 3^2 \times 11$.

Find

(a) the value of the cube root of q,

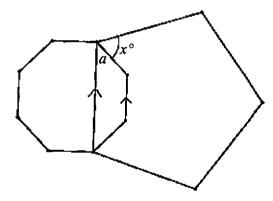
(b) the LCM of p, q and r, giving your answer as the product of its prime factors,

(c) the greatest number that will divide p, q and r exactly.

The greatest number =
$$HCF = 2^2 \times 3 = 12$$

Answer[1]

13 The diagram shows a regular pentagon and a regular octagon. Calculate the value of x.



Each interior angle of pentagon = $\frac{(5-2)}{5} \times 180^{\circ}$

Each interior angle of octagon = $\frac{(8-2)}{8} \times 180^{\circ}$ = 135°

$$a = \frac{1}{2} (360^{\circ} - 2 \times 135^{\circ}) (\angle \text{ sum of isosceles trapezium})$$

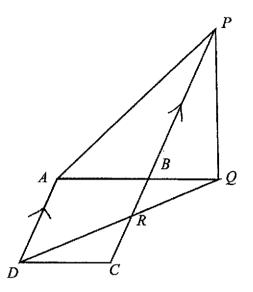
= 45°

$$x^{\circ} = 108^{\circ} - 45^{\circ}$$

= 63°

Turn over

14 The diagram shows a rhombus ABCD. ABQ, PBC and DRQ are straight lines and AQ = BP.



(a) State the triangle that is similar to triangle BRQ.

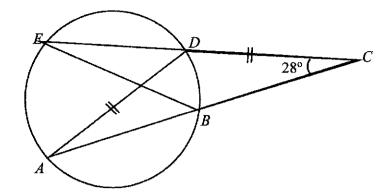
Triangle ADQ or Triangle CRD

Answer Triangle[1]

(b) Prove that triangle DQA is congruent to triangle APB.

AD = AB (given ABCD is a rhombus) angle DAQ =angle ABP (alternate angles, AD parallel to BC and BP) AQ = BP (given) Therefore triangle DQA is congruent to triangle APB. (SAS)

[2]



A, B, D and E are points on the circle such that AD = CD and angle $BCD = 28^{\circ}$. Explain with geometrical reasons, why the length of BC equals to BE.

Angle $DAC = 28^{\circ}$ (base angles of isosceles triangle ACD)

Angle DEB = Angle DAC (angles in same segment)

 $= 28^{\circ}$

= Angle BCD

So triangle BCE is an isosceles triangle.

Therefore the length of BC equals to BE.

Many students are not able to spell the word **isosceles** correctly.

[3]

The masses of 20 bags, in kg, are measured.The results are shown on the stem-and-leaf diagram.

Mass of 20 bags

Stem	Leaf
0	9
1	2
2	0666
3	0 3 3 4 4 8 8 1 2 9 9 9
4	12999
5	0 1

Key: 0|9 means 0.9 kg

(a) Find the mean mass of the bags.

Mean mass =
$$\frac{69}{20}$$
 kg
= 3.45 kg

A few forgot to check the key and did not realise the decimal point, hence giving the answer as 34.5 kg which is incorrect.

Answer	kg	[1]
7 T 1 M 7 T 1 W 1		

(b) Find the standard deviation of the masses of the bags.

Standard deviation =
$$\sqrt{\frac{266.8}{30} - 3.45^2}$$
 kg
=1.20 kg (3 s.f.)

	•	F 4	
Answer	kg	HJ	L

(c) It was found later that the weighing machine has an error.

Each bag was actually 0.08 kg heavier.

Explain how this will affect the mean and standard deviation.

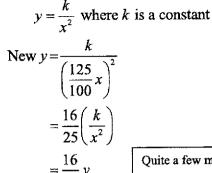
Answer

The mean will increase by 0.08 kg.

The standard deviation will remain the same.

[2]

(a) If x is increased by 25%, find the percentage change in y.



Percentage change = $\frac{new - original}{original} \times 100\%$

Percentage change in
$$y = \frac{\frac{16}{25}y - y}{y} \times 100\%$$

ed the negative sign = -36%

Quite a few missed the negative sign as it is a decrease in y.

Answer% [2]

- **(b)** Given that y = 16 when $x = \frac{1}{2}$, find
 - (i) the equation connecting y and x,

$$k = yx^{2}$$

$$= 16\left(\frac{1}{2}\right)^{2}$$

$$= 4$$

$$\therefore y = \frac{4}{x^2}$$

Answer[2]

(ii) the value of x when y = 100.

When y=100,

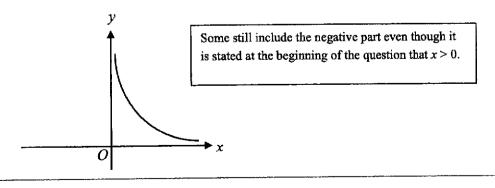
$$x^2 = \frac{4}{100}$$
$$= \frac{1}{25}$$
$$x = \frac{1}{5}$$

Some forgot to reject the negative value as it is given at the beginning of the question that x > 0.

Answer x = [2]

(c) Sketch the graph which represents the relation between y and x.

[1]



18 In the following sequence,

[Turn over

$$(1 \times 2) - 2 = 0$$

 $(2 \times 3) - 4 = 2$
 $(3 \times 4) - 6 = 6$
 $(4 \times 5) - 8 = 12$
......
 $(a \times 12) - b = c$
......
 $(d \times e) - f = g$

(a) Find the values of a, b and c.

$$a=11$$
 $b=2\times11$ $c=11\times12-22$ $=22$ $=110$ Answer $a=..., b=..., c=...$ [2]

(b) Express g in terms of d.

e = d + 1

$$f = 2d$$

$$g = d(d+1)-2d$$

$$g = d^2 + d - 2d$$

Some left out the "g = "part in their answer blank which is part of the required answer.

 $g = d^2 - d$ g = d(d-1)

Answer[2]

(c) Explain why 279 cannot be the result of an equation in this sequence.

Answer [1]

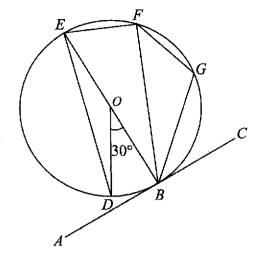
g is the product of an odd and an even number. Therefore g must be even. Since 279 is odd, 279 cannot be the result of an equation.

Alternatively,

$$279 = 9 \times 31$$

From (b), g is the product of 2 consecutive integers which is an even number. 279 is odd, therefore 279 cannot be the result of an equation in this sequence.

The diagram shows a circle BDEFG, centre O and diameter BE. The line AC is a tangent to the circle at B and angle $BOD = 30^{\circ}$. The ratio of angle EBF to angle FBG to angle GBC is 1:1:2.



(a)	State a	fact	about	the	arcs	EF	and	FG
-----	---------	------	-------	-----	------	----	-----	----

Answer Arc EF = Arc FG[1]

- (b) Showing all reasons clearly, find
 - (i) angle DEB,

angle $DEB = 15^{\circ}$ (angle at centre = 2 × angle at circumference)

Answer[1]

(ii) angle EFG.

angle $EBC = 90^{\circ}$ (tangent perpendicular to radius)

angle
$$EBG = \frac{2}{4} \times 90^{\circ}$$

= 45°

angle
$$EFG = 180^{\circ} - 45^{\circ}$$
 (angles in opposite segments)
=135°

Some are still not using the standardised geometrical reasons/statements for stating the reasons.

Students must use only the given standardised geometrical properties/reasons.

Some are using very long-winded methods even though it is only 2 marks.

Answer[2]

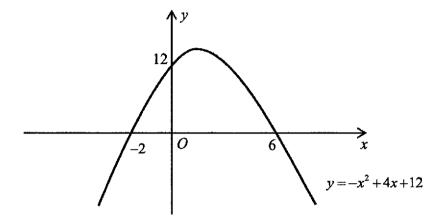
[Turn over

20 (a) Express $-x^2 + 4x + 12$ in the form -(x+p)(x-q).

$$-x^2 + 4x + 12 = -(x^2 - 4x - 12)$$
$$= -(x+2)(x-6)$$

Answer	***************************************	1	1

(b) Sketch the graph of $y = -x^2 + 4x + 12$ on the axes below. Indicate clearly the values where the graph crosses both axes. [2]



(c) Find the coordinates of the turning point.

Turning point is (2, 16).

(d) Without solving the equation algebraically, explain why $-x^2 + 4x + 12 = 18$ has no solution.

Since the maximum value of the curve y is 16, there is no point of intersection between the curve and the horizontal straight line y = 18.

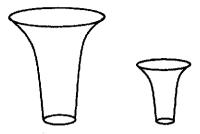
Or

The line y = 18 is always above the curve, so there is no point of intersection between the curve and the straight line y = 18.

Answer	•••••	 *********	 	

Some are still using algebraic method to solve despite the instruction saying otherwise.

21 The diagram shows two geometrically similar containers. The cost of painting the base area of the smaller container is $\frac{25}{64}$ of the cost of painting the base of the larger container.



(a) The top of the larger container has a circumference of 24 cm. Find the circumference of the top of the smaller container.

$$\left(\frac{l_s}{l_l}\right) = \sqrt{\frac{25}{64}} = \frac{5}{8}$$

Circumference of the top of smaller container = $\frac{5}{8} \times 24$ = 15 cm

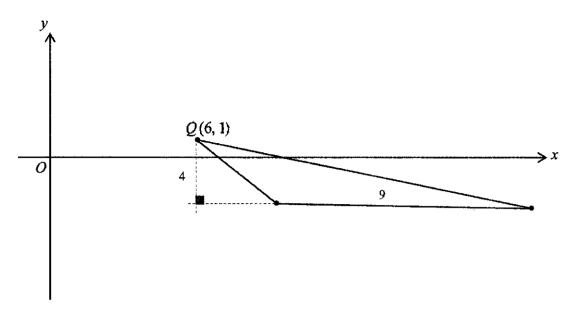
Answer	************	cm	[2
21/10///	***************************************		L

(b) The capacity of the smaller container is 0.45 litres.
Find the capacity of the larger container, giving your answer to 2 decimal places.

Capacity of the larger container
$$=$$
 $\left(\frac{8}{5}\right)^3 \times 0.45$ litres
= 1.8432 litres
= 1.84 litres (2 decimal places)

Answer		litres	[1]
--------	--	--------	-----

22



In the diagram, the points P, Q and R have coordinates (9,-3), (6,1) and (18,-3)respectively.

(a) Find the length of PQ.

$$PQ = \sqrt{(9-6)^2 + (-3-1)^2}$$

$$= \sqrt{3^2 + (-4)^2}$$
= 5 units

Answer	units	۲1
22110 1101	······································	

Find the value of $\cos \angle QPR$, giving your answer as a fraction in its simplest form. **(b)**

$$\cos \angle QPR = -\frac{3}{5}$$
 Some could not identify the right - angled triangle and some forget that $\cos A = -\cos \left(180^{\circ} - A\right)$

Answer[1]

Find the area of triangle PQR. (c)

Area of triangle $PQR = \frac{1}{2} \times 9 \times 4 \text{ units}^2$

$$=18 \text{ units}^2$$

Some are using other more time-consuming methods such as "shoelace", $\frac{1}{2}ab\sin C$ even though the question is only 1 mark.

Answer[1]

(d) Find the equation of the line PQ.

Gradient of
$$PQ = \frac{1 - (-3)}{6 - 9}$$
$$= -\frac{4}{3}$$

Equation of *PQ* is
$$y-1=-\frac{4}{3}(x-6)$$

 $y-1=-\frac{4}{3}x+8$
 $y=-\frac{4}{3}x+9$ or $4x+3y=27$

Answer[2]

(e) The equation of the line passing through the point R is 4x + 21y = 9. Find the coordinates of the point of intersection of this line and the line PQ.

... The point of intersection is $\left(7\frac{1}{2}, -1\right)$.

Students must remember to put the brackets for the coordinates on their answer blank.

Answer[3]

~ End of Paper ~

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Name:	Class:	Class Register Number:





CHUNG CHENG HIGH SCHOOL (MAIN)

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PRELIMINARY EXAMINATION 2021 SECONDARY 4

MATHEMATICS

4048/02

Paper 2

Wednesday 1 September 2021
2 hours 30 minutes

Candidates answer on the Question Paper

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use paper clips, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown with the answer. Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate. If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 100.

For Examiner's Use					
Question Number	Marks Obtained				
1					
2					
3					
4					
5					
6					
7					
8					
9					
10					
Total Marks					

This document consists of 21 printed pages and 1 blank page.

Mathematical Formulae

Compound interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = $\pi r l$

Surface area of a sphere = $4 \pi r^2$

Volume of a cone =
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere =
$$\frac{4}{3}\pi r^3$$

Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

Arc length = $r\theta$, where θ is in radians

Sector area =
$$\frac{1}{2}r^2\theta$$
, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

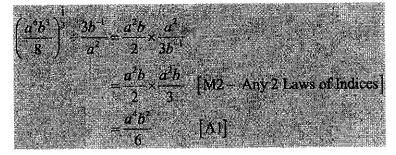
$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$Mean = \frac{\Sigma fx}{\Sigma f}$$

Standard deviation =
$$\sqrt{\frac{\Sigma f x^2}{\Sigma f} - \left(\frac{\Sigma f x}{\Sigma f}\right)^2}$$

1 (a) Simplify
$$\left(\frac{a^6b^3}{8}\right)^{\frac{1}{3}} \div \frac{3b^{-1}}{a^2}$$
.



Answer[3]

(b) Solve
$$\frac{2}{x-2} + \frac{3}{x+2} = 0$$
.

$$\frac{2(x+2)+3(x-2)}{|(x-2)(x+2)|} = 0$$

$$\frac{2(x+2)+3(x-2)}{|(x-2)(x+2)|} = 0$$

$$\frac{2x+4+3x-6=0}{|(x-2)(x+2)|} = 0$$

Answer $x = \dots$ [2]

(c) Make q the subject in the equation $pq+9=p^2+3q$ and simplify your answer.

$$pq + 9 = p + 3q$$

$$pq = 3q = p^p - 9$$

$$q(p-3) = (p-3)(p+3)$$

$$p = \frac{p-3}{p-3}$$

$$q = p+3$$

$$[Mi = Grouping q, terms]$$

$$p(m-3) = \frac{p-3}{p-3}$$

$$q = p+3$$

Answer[3]

(d) (i) Simplify $(4x+3y)^2 + (3x-4y)^2$.

$$(4x+3y)^{2} + (3x+4y)^{2}$$

$$= 16x^{2} + 24xy + 9y^{2} + 9x^{2} - 24xy + 16y^{2}$$
 [MI— Expansion]
$$= 25x^{2} + 25y^{2}$$

$$= 25(x^{2} + y^{2}).$$
 [AI]

Answer[2]

(ii) It is given that $x^2 + y^2 = 1$. Using your answer in part (i), explain why the maximum value of $(4x + 3y)^2$ is 25.

$$(4x+3y)^{2} + (3x-4y)^{2} = 25(x^{2}+y^{2})$$

$$= 25(1) \qquad \left[\sqrt{M1} - \text{Substitute for } x^{2} + y^{2} = 1\right]$$

$$= 25$$

$$(4x+3y)^{2} = 25 - (3x-4y)^{2} \qquad \left[B1\right]$$
Since $(3x-4y)^{2} \ge 0$, $-(3x-4y)^{2} \le 0$ [A1—Recognising that $(3x-4y)^{2} \ge 0$]
$$25 + (3x-4y)^{2} \le 25$$

$$(4x+3y)^{2} \le 25$$
Max value of $(4x+3y)^{2} = 25$ (shown) [AG]

5

2 During nuclear fusion, it is observed that when two hydrogen atoms are fused together to form one helium atom, there is a loss in mass, M.
The atomic masses of one hydrogen atom and one helium atom are given in the table below. The masses are given in atomic mass unit (u).

Atom	Hydrogen	Helium
Atomic Mass (u)	2.0141	4.0026

(a) Find M (in u), leaving your answer in standard form.



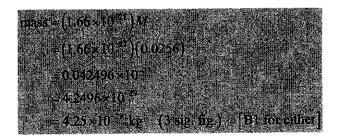
Answer u [2]

(b) Express M as a percentage of the atomic mass of one helium atom.



Answer% [2]

(c) Given that $1 u = 1.66 \times 10^{-27} \text{ kg}$, find M in kilograms.



Answerkg [1]

[Turn Over

- 3 Town P and Town Q are 40 km apart. A car is travelling from Town P to Town Q at an average speed of x km/h. During its return journey, the car later travelled back to Town P from Town Q at an average speed of (x+8) km/h and the time taken for the return journey was 12 minutes less.
 - (i) Write down an equation to represent this information and show that it simplifies to $x^2 + 8x 1600 = 0$.

 Answer

$$\frac{40}{x} \frac{40}{x+8} = \frac{1}{5} \quad [M1-Correct expression for time (either)]$$

$$\begin{bmatrix} B1-Forming equation with \frac{1}{5} \\ \frac{1}{5} \end{bmatrix}$$

$$\frac{40(x+8)-40x}{x(x+8)} = \frac{1}{5} \quad [M1-Single fraction]$$

$$\frac{320}{x^2+8x} = \frac{1}{5} \quad [M1-Simplifying]$$

$$x^2+8x=1600$$

$$x^2+8x-1600=0 \quad (shown) \quad [AG]$$

[4]

(ii) Solve the equation $x^2 + 8x - 1600 = 0$, giving your solutions correct to two decimal places.

$$x^{2} + 8x - 1600 = 0$$

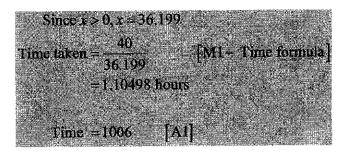
$$x = \frac{-8 \pm \sqrt{8^{2} - 4(1)((-1600))}}{2(1)}$$

$$= \frac{-8 \pm \sqrt{6464}}{2}$$

$$x = 36.199 \text{ or } x = -44.199$$

$$x = 36.20 \text{ or } x = -44.20 \text{ (2 dec. places)} \text{ [A1 each]}$$
Note: -1 mark if left in 3 sig. fig.

 (iii) Given that the car left Town P at 0900, find the time when the car reached Town Q. Give your answer correct to the nearest minute.



Answer[2]

The variables x and y are connected by the equation $y = \frac{3}{2}x + \frac{5}{x} - 7$. Some corresponding values of x and y are given in the table below.

x	0.5	1	1.5	2	3	4	5	6	7
у	3.75	-0.5	-1.42	р	-0.83	0.25	1.5	2.83	4.21

(a) Find the value of p.

-1.5 B1

(b) On the grid opposite, draw the graph of $y = \frac{3}{2}x + \frac{5}{x} - 7$ for $0.5 \le x \le 7$.

Use the scale of 2 cm to represent 1 unit on both axes.

[3]

[1]

(c) By drawing a tangent, find the gradient of the curve at x = 2.5.

From graph,

Drawing tangent [M1]

Gradient = 0.7 [0.6-0.8] [A1]

Answer[2]

(d) (i) On the grid in part (b), draw the line 2y + x = 2 for $0 \le x \le 7$.

$$2y + x = 2$$

$$2y = -x + 2 \qquad [M1 - Make y the subject]$$

$$y = -\frac{1}{2}x + 1 \quad [G1 - Draw y][G2 - If draw graph only]$$

[2]

(ii) Write down the x-coordinates of the points where the line intersects the curve.

$$x = 0.75 [0.7 - 0.8], x = 3.25 [3.2 - 3.3] [A1]$$

Answer x = or [2]

(iii) Show that the points of intersection of the line and the curve give the solutions to the equation $2x^2 - 8x + 5 = 0$.

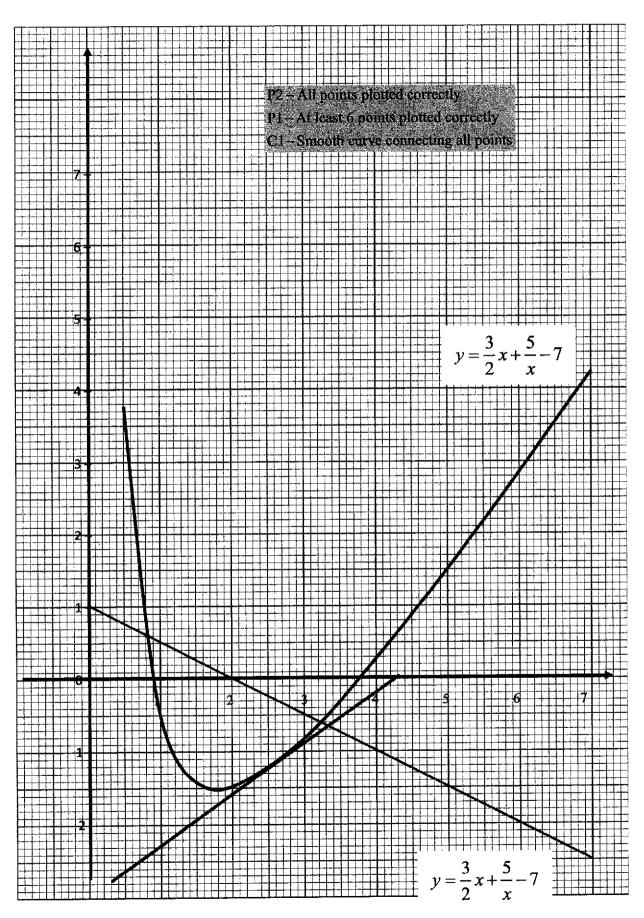
$$\frac{3}{2}x + \frac{5}{x} - 7 = \frac{1}{2}x + 1 \qquad [M1 - Equating]$$

$$3x^{2} + 10 - 14x = -x^{2} + 2x$$

$$4x^{2} - 16x + 10 = 0 \qquad [A1]$$

$$2x^{2} - 8x + 5 = 0 \qquad [AG]$$

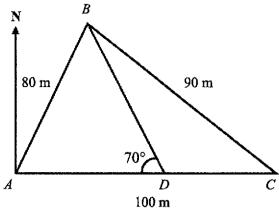
Answer[2]



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5 The diagram below shows three points, A, B and C on flat ground.

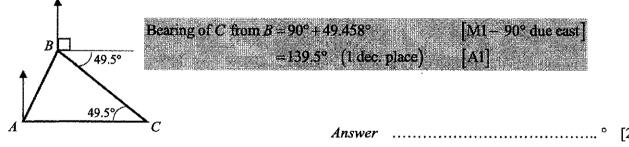
AB = 80 m, AC = 100 m and BC = 90 m. C is due east of A.



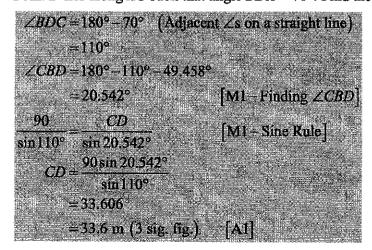
(a) (i) Show that angle $ACB = 49.5^{\circ}$, correct to one decimal place.

$$\cos \angle ACB = \frac{90^2 + 100^2 - 80^2}{2(90)(100)}$$
[MI]—Cosine Rule or other method]
$$\angle ACB = \cos^{-1} \left(\frac{90^2 + 100^2 - 80^2}{2(90)(100)} \right)$$
[MI]—Cosine Rule or other method]
$$= 49.458^{\circ}$$
[A1]
$$= 49.5^{\circ}$$
(shown)

(ii) Hence, calculate the bearing of C from B.



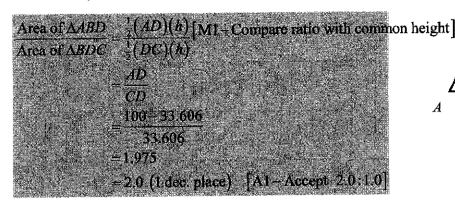
(iii) Point D lies along AC such that angle $BDA = 70^{\circ}$. Find the distance CD.

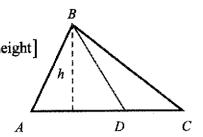


Answer m [3]

(iv) Find the ratio of area of triangle ABD to area of triangle BDC. Give your answer correct to one decimal place.

Since they share a common height,

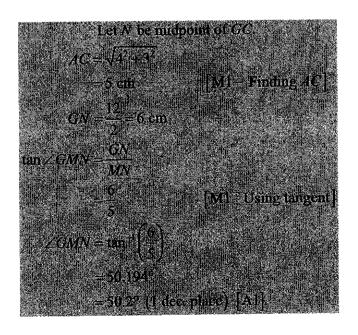


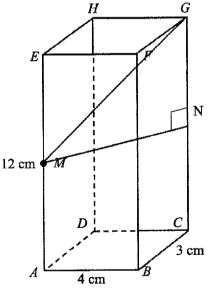


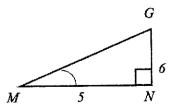
4		[2]
4nswer	****************	[4]

(b) The diagram below shows a cuboid with rectangular base ABCD. AB = 4 cm, BC = 3 cm and AE = 12 cm. M is the midpoint of AE.

Find the angle of elevation of G from M.



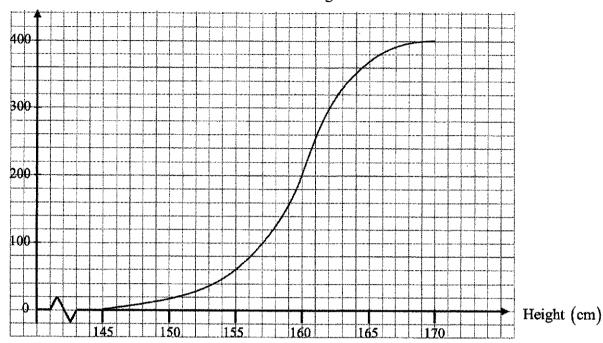




Answer[3]

Turn Over

6 (a) The heights of 400 students in School A are recorded. The cumulative frequency curve below shows the distribution of their heights.



(i) State the median.

Cumulative frequency

160 cm [B1]

(ii) Find the interquartile range of the distribution.

$$Q_i = 157, Q_i = 162$$

$$IQR = 162 - 157 [B1]$$

$$= 5 \text{ cm} \qquad [B1]$$

(iii) In School B, the median and interquartile range of the heights of another 400 students are 165 cm and 8 cm respectively. Make two comments comparing the heights of students in School A and School B.

Answer

The students in School B are generally taller as they have a higher median of 165 cm as compared to School A (160 cm).

The height of students in School B are generally more widespread as they have a

higher interquartile range of 8 cm as compared to School A (5 cm). [B1 each]

[2]

(b) John flipped a coin five times and obtained five successive heads. Is it conclusive that the coin is biased? Explain your answer clearly.

Answer

No, given that John only flipped the coin 5 times, there is a 1 in 32 chance that of obtaining 5 successive heads which is still possible. The sample size is **too small** for any logical conclusion that the coin is biased.

[2]

(c) A two-digit number is formed by drawing a random card from Bag A followed by another random card from Bag B. Bag A contains three cards labelled '1', '2' and '3'. Bag B contains three cards labelled '4', '5' and '7'. For example, drawing a '1' and "5" from Bag A and Bag B respectively will form the number '15'.

(i) Complete the possibility diagram below.

Any	Lexi		44	\mathbf{n}
	3.00			
4 11			. r	tsol
All r	DWS ((0)31(2)	74 - [P4]

$Bag B \setminus Bag A$	1	2	3
4	14	24	84
5	5	25	
7	¥	27	37

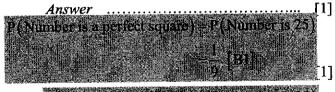
[2]

Find, as a fraction in its simplest form, the probability that the two-digit number formed is

(ii) odd,

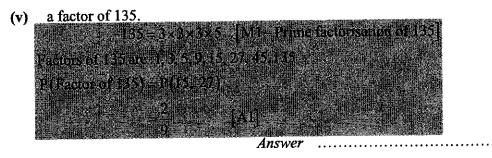


(iii) a perfect square,



(iv) a prime number,

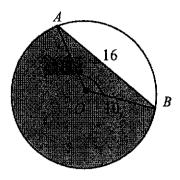




Turn Over

[2]

7 The diagram shows a circle, centre O, radius 10 cm. AB is a chord of length 16 cm.



(a) Show that angle AOB = 1.855 radians, correct to four significant figures.

Answer

$$\sin \frac{\angle AOB}{2} = \frac{8}{10}$$

$$\angle AOB = 2\sin^{-1}\frac{8}{10}$$

$$= 1.8545$$

$$= 1.855 \text{ rad. (shown) [AG]}$$

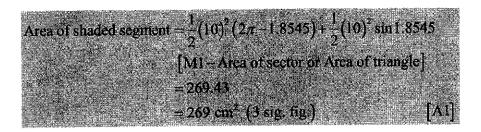
[2]

Hence, find the

(b) perimeter of the shaded segment,

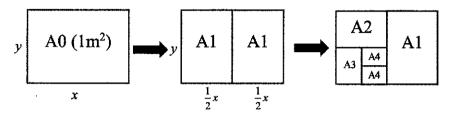
Perimeter =
$$(2\pi - 1.8545)(10) + 16$$
 [M1, M1]
= 60.28
= 60.3 cm (3 sig. fig.) [A1]

(c) area of the shaded segment.



 8 A piece of A0-sized paper has a total surface area of 1 m². The length and breadth of the A0-sized paper are x m and y m respectively.

An A1 paper is an A0 paper folded in half, length-wise. An A2 paper is an A1 paper folded in half, so on and so forth.



(i) Write down the relationship between x and y.

$$xy = 1$$
 [B1 oc]
$$Answer \qquad [1]$$

Given that all A-sized papers are geometrically similar, show that $\frac{x}{y} = \sqrt{2}$.

Since the papers are geometrically similar, ratio of corresponding sides are equal.

$$\frac{length_{A0}}{breadth_{A0}} = \frac{length_{A1}}{breadth_{A1}}$$

$$\frac{x}{y} = \frac{y}{\left(\frac{1}{2}x\right)} = [M1 \text{ or similar}]$$

$$\frac{x^2}{y^2} = 2 \qquad [A1]$$

$$\frac{x}{y} = \sqrt{2} \text{ (Shown)} \quad [AG]$$

[2]

(iii) Hence, using parts (i) and (ii), find the values of x and y.

$$y = \frac{1}{x} - - - - (1) \qquad [M1 - Making x \text{ or } y \text{ the subject}]$$

$$\frac{x}{y} = \sqrt{2} - - - (2)$$
Substitute (1) into (2):
$$\frac{x}{y} = \sqrt{2}$$

$$\frac{x}{y} = \sqrt{2}$$

$$x = \sqrt{2}$$

$$x = \sqrt{2}$$

$$x = \sqrt{2}$$

$$x = \sqrt{2}$$

$$x = 1.1892$$

$$x = 1.19$$

$$y = 0.841 \quad (3 \text{ sig fig}) \quad [A1 - Both answers correct]$$

[4]

(iv) Write down the dimensions of an A4-sized paper in millimetres.

1.1892×1000			
= 297 (3 sig fig) [
and Copper to a	All Control of		
$y = \frac{0.84089 \times 1000}{1000}$			
= 210 (3 sig fig))	* * * * * * * * * * * * * * * * * * *	asaa II Dh	
= EXM Table 1/R11	At-Bom.	mircellina.	Domination

<i>Answer</i> mm × mr	n [2]
-----------------------	-------

(v) Given that N is an integer, express the number of pieces of AN-sized paper that can be cut out from an A0-sized paper in terms of N.

Number of pieces
$$= 2^k \cdot [B1]$$

4		F17
Answer	***********	[T]

9 Robert has 3 options to get to school every weekday morning.

Option A: He takes the bus.

Option B: He takes the MRT.

Option C: He takes a taxi.

The matrices A, B and C represent his journey to school if he were to choose option

A, B or C respectively.

	Bus	MRT	Taxi	Bus	MRT	Taxi	Bus	MRT	Taxi
	(1	0	0)	0	0 -	0	(0	0	0)
A =	0	0	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$, B =	0	1	0 , C=	= 0	0	0 .
	0	0	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	0	0)	0	0	1

(a) In a particular week, Robert took the bus 3 times. He took the MRT and taxi in each of the other two days. The above information can be represented by a matrix S where S = 3A + B + C. Find S.

$$S = 3 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} + \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} + \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
 [M1]
$$= \begin{pmatrix} 3 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
 [A1]

	•	
Answer		[2]
answei		121

(b) The table below shows the travelling time taken, in minutes, for each of the 3 options that Robert can take to get to school.

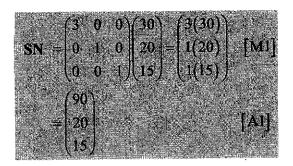
Option	Bus	MRT	Taxi
Time taken (in minutes)	30	20	15

(i) Write down a column matrix N to represent the information in the table.

$$\mathbf{N} = \begin{pmatrix} 30 \\ 20 \\ 15 \end{pmatrix} \quad \begin{bmatrix} \mathbf{B1} \end{bmatrix}$$

Answer
$$N = \dots$$
 [1]

(ii) Evaluate the matrix SN.



	Answer $SN = \dots$	[2]
(iii)	State what the elements in matrix SN represent. Answer	
	The elements represent the total time taken in minutes, in that particular	
	week by Robert to go to school by via option A, B and C respectively.	
		[1]
	e down a matrix J such that product of J and the answer in part (b)(ii) will the average travelling time taken by Robert in a particular week.	F.1
	0.2 0.2 0.2) [Al-Accept fractions]	
Uana	Answeree, find the average travelling time taken by Robert per day in a particular	[1]
110110	o, that the average materials white the of record per any of	

..... minutes Answer

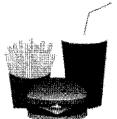
[2]

(c)

(d)

week.

10 The diagram below shows the menu from a fast food restaurant.



Combo A

- Burger
- Medium Fries
- Medium Drink

\$5.90 only!

Upsize your drink and fries to Large-size for only \$1.<u>10</u>

Ala carte	Medium (\$)	Large (\$)	
Burger (1 size)	3.20		
Fries	2.20	2.90	
Drink	2.80	3.60	

(a) Albert wants to buy a burger for both himself and his brother Bart. His brother wants at least a medium-sized fries. Albert wants a large drink while Bart wants a medium drink.

By considering three options, suggest how Albert should place his order. Justify any decisions that you make and show your calculations clearly.

Answer

Choose 3 out of the 4 possible options

Option C:
$$2 \times Burger + M$$
. Fries $+ M$. Drink $+ L$. Drink Total cost $= \$2(3.20) + 2.20 + 2.80 + 3.60$

$$= \$15.00$$

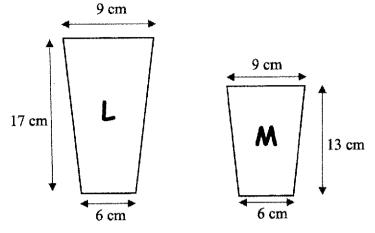
$$[B1]$$

He should choose Option D to minimise his spending [B1—Correct Option with logical and reasonable explanation]

[4]

OR He should choose Option C as for \$0.20 more, he can get an extra packet of medium fries so it is the most value – for – money option.

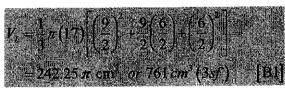
(b) The diagram below shows the cross-sectional area of the large (L) and medium (M) drink cups sold by the fast food restaurant in part (a). The Large and Medium cups have a height of 17 cm and 13 cm respectively. The top and bottom diameters of both cups are 9 cm and 6 cm respectively



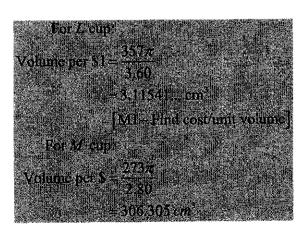
The volume of a cup is given by $V = \frac{1}{3}\pi h(R^2 + Rr + r^2)$ where h is the height,

R and r are the radii of the top and bottom of the cup respectively. Using the information from part (a), determine whether the medium cup or large cup gives better value for money.

Answer







OR

E 17

Ry comparing ratio:

13 117

[M1 Gomparing ratio]

14 17 13 91

[M1 Gomparing ratio]

15 17 110

[M1 Gomparing ratio]

16 17 17 18 91

[M2 Gomparing ratio]

17 18 91

[M2 Gomparing ratio]

:. Large cup gives more value for money [A1]

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